# Exploring the Motion Manifold for an Articulated Arm UGP Presentation

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- Introduction
- Related Work
  - Motion planning of planar robots
- Oata Generation
- 4 Challenges
  - Visualizing the motion manifold
    - Ideal motion manifold
    - Manifold generated on Images
- Proposals
  - Analysis
  - Proposals

#### Introduction

#### Ultimate Aim of the Work

Plan paths of multiple robots.

#### Aim of this Project

Extension of motion planners to 3-D with the help of **simulations** 

- This project is an extension of the M. Tech. thesis of Debojyoti Dey [Dey, 2015] from 2 dimensions to 3 dimensions
- Requires exploration of motion manifold using only visual input

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## Motion planning for planar robots

Have a look at the video demonstrations of Debojyoti's algorithm.

## Motion planning for planar robots

- Visual Configuration Space
- Decoupled road-map composition
- Probabilistically resolution complete

#### 3D Articulated Arm

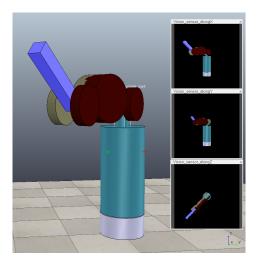


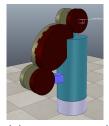
Figure: Robotic arm with 3 revolute joints - Created in v-rep. The 3 smaller windows show the image captured by the vision sensors installed in the scene (image has been generated using v-rep software)

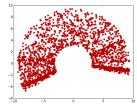
#### **Data Generation**

Images captured during simulation.

Advantage: Avoids impossible poses

Disadvantage: Loss of uniformity in randomness

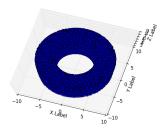




(a) An impossible (b) Plot showing pose generated by accumulation of data points assigning random on the boundaries (Details: angles to all the joints  $\begin{array}{c} \text{Radial distance} = 2\pi + \theta_2, \\ \text{and angle} = \theta_0 ) \end{array}$ 

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#### Ideal Motion Manifold



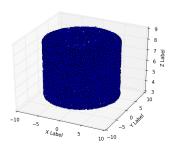
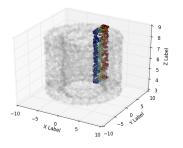
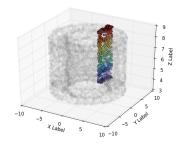


Figure: 3-D plot of  $\theta_0, \theta_1$  and  $\theta_2$  is a hollow cylinder (*Details*:  $2\pi + \theta_0 = distance$  from z-axis,  $2\pi + \theta_1 = distance$  from x-y plane &  $\theta_2 = angular$  displacement along z-axis)

#### Ideal Motion Manifold





(a) color changes as  $\theta_0$  increases

(b) color changes as  $\theta_1$  increases

Figure: 3-D plots explaining the structure of the hollow cylinder in figure 2 (Details: The colored points only correspond to configurations which have  $0 < \theta_2 < 0.1 \text{ rad}$ )

## Manifold Generated on Images

We used ISOMAP (Stanford University's MATLAB code) to generate this from the image data:

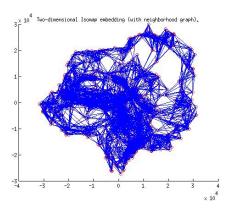


Figure: 2-D projection of the configuration-space of the robot, as deduced by dimensionality reduction using ISOMAP

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## **Analysis**

#### Major reasons of these short-circuits:

- a jump when 2nd link and the base cylinder are in the same spatial region (Figure 5).
- the opposite faces of the middle link get inter-changed ( $\theta_1$  change by 180°, and  $\theta_2$  and  $\theta_3$  change signs) (6).

## Short-circuits: Type 1

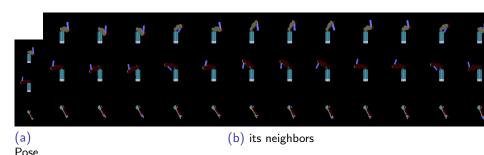


Figure: Illustration of a short-circuit: Poses in which the 3rd link is in the same spatial region, but the angles are far off, also become neighbours [ $\Delta\theta_2\sim0$ ;  $\Delta\theta_1\sim60^\circ-100^\circ$ ;  $\Delta\theta_0\sim180^\circ$ ]

## Short-circuits: Type 2

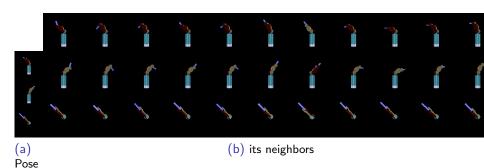


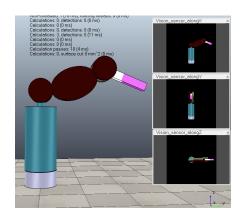
Figure: Illustration of a short-circuit: Poses which occupy approximately the same space, but are far off in the actual manifold become neighbours [ $\Delta\theta_2=180^\circ$ ,  $\Delta\theta_1=-2\theta_1$  &  $\Delta\theta_0=-2\theta_0$ ]

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### **Proposals**

- Changes in input image
- Change in distance metric (use of Ideal Track Points [Ramaiah et al., 2015])



## Bibliography I



Visual Motion Planning of Multiple Robots by Composing Roadmaps. Master's thesis, IIT Kanpur, India.

Ramaiah, M. S., Mukerjee, A., Chakraborty, A., and Sharma, S. (2015).

Visual generalized coordinates. *CoRR*, abs/1509.05636.

## APPENDIX - A

Explanation of the key traits of Debojyoti's algorithm

## Visual Configuration Space

Traditional methods used Motion configuration Space.

- Planning path on a configuration space defined in terms of motion parameters becomes intractable when the dimension of the configuration space grows up
- Dimension of visual configuration space is independent of degrees of freedom of the robots.

## Multi-robot Motion Planning

- Centralized Path Planning
- Decoupled Path Planning

## Multi-robot Motion Planning

- Centralized Path Planning
- Decoupled Path Planning
  - Prioritized planning
  - Fixed-path coordination
  - Semi centralized model
  - Fixed road-map coordination

## Probabilistically Resolution Complete

Completeness

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- Completeness
- Probabilistic completeness

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- Probabilistic completeness
- Resolution completeness

# APPENDIX - B

Another Major Challenge: Completeness

Completeness

## Challenge: Correctness and Completeness

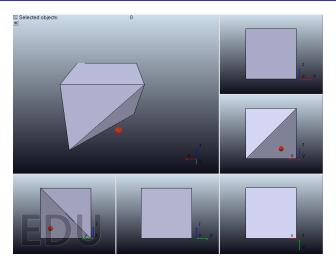


Figure: (left-top)A small sphere near a truncated cube; (others) all 5 cameras (placed at orthogonal positions) detect "false" collision (image has been generated using v-rep software)